Abstract structures, which are the topics of mathematics and which take part in Popper's World 3 are created or discovered - this depends on the philosophical meaning - by the human mind. They are inspired both by perception and rational reflection and sometimes moreover by an aesthetic feeling, so e.g. Platon's explanations in "Timaeus" construct the theory, that triangles and minimal euclidian solids are the first components of the physical world.

Let's start now from the point, where we accept the existence of abstract algebraic, topologic etc. structures. In an integral way of thinking analogies play an important role, and under this proposition it is ingenious to discover analogies between mathematical structures and structures of music. The central theorem of the statement, the author holds is, that those analogies are not a priori but must be based on a special way of constructing them. In algebra something like this (in a very strong way) is called isomorphism.

In a very similar way isomorphisms or principles of transformations can be created, so that it is possible to say, that two objects, e.g. algebraic structures and musical events, show analogies. Here three kinds of such isomorphisms are explained and explored as a basis of pedagogical reflections: a formal, an aesthetic-heuristic and a depth-psychological one.

1. The formal isomorphism:
   Let us take an algebraic structure, especially a symmetric group. We want to create a formal isomorphism between this group and music.
   1.1. First the question arises, which elements here should be adjoined to which elements there. Concerning the groups we take "permutations", the real elements of the group, concerning music we choose pitches of a note. This is totally arbitrary thus it would also have been possible to choose special rhythms, the duration of notes etc. This is the step, where we regulate the objects, we deal with.
   1.2. The next problem is the range of the notes, quasi a kind of mode. In an example already put into practice we worked with the symmetric group $S_4$, which has 24 elements. It seemed to be natural to take either an octave divided into 24 quartenotes or a chromatic scale over the range of two octaves. With regard to the possibilities of the school, the second way has been chosen, so that it was possible to make experiences with classic instruments.
   1.3. The next problem is the fixing of the coordination between group-elements and the pitches. Like the former stipulations also the solution of this problem is arbitrary, perhaps heuristically influenced. The modus, which was taken in our pedagogic process was influenced in this manner: (1234) was adjoin to C (the identity), (1243) to Cis, (1324) to D, (1342) to Dis etc. This yields a mathematical function between the set of the elements of the symmetric group $S_4$ an the notes of the
The next question is what to do with this function. First it is intended to form music which is connected with the structure of the symmetric group S₄. There two fundamental ideas were found:

1.4.1 A group has special sub-structures, especially subgroups, that is to say those subsets, which build together with the group-defining multiplication a group too. According to the fixed function these subgroups yield special accords. These can create a set of themes on which improvisations may be based.

1.4.2 The multiplication of two group-elements is a well defined group element. Now we can begin with some subset of the set of group elements. This means beginning our piece of music with a special accord. Each element of our subset can be multiplied with another element of this subset, so that the set of all possible multiplications is a new accord, which has been created by the former accord. A set of three elements normally forms another a set of three elements (a result of two elements is possible, too). This set yields a new one and so on. The piece is (not in the rhythmic way) totally determined by the beginning accord.

1.5 In our pedagogic process these reflections were fundamental. First the pupils learned that analogies do not exist without depending on special identification rules. Analogies are built by the human mind, or at least, only these analogies are - in the sense of Kant recognizable by a human being.

The next step was the recognition of the possibility to transform algebraic structures (which are beautiful in a special sense) to sound, a possibility, which is in a special sense much more determined than a piece based on a heuristically built dodekaphone trope.

The next pedagogic sequence is based on the improvisation over this sound-structures, where both possibilities 1.4.1. and 1.4.2. are practised.

2. The aesthetic-heuristic isomorphism:
Intermedial transformations are a central problem of polyaesthetical education. This chapter can be submitted to this field of questions. You can try, once having understood the structure of symmetric groups (as well as other abstract structures), to transform them to a piece of art, to music, to concrete poetry etc. This demands a complex act of creativity and depends moreover both on the cultural experience of the transforming individuum and the internally represented adventure of the moment.

Here the transformed results are not formally determined but must be explored in regard to their social and psychic, and sometimes semantically influenced, sources, especially those that are highly relevant for arts.

This aspect completes the process as a pedagogic one, in which the pupils exercises his abilities in creative problem solving activities (especially in both an artspecific and an abstract way, the latter sometimes influencing the creativity in respect to other problems) and cultivates his experiences with the arts.

Moreover there processes concern not only a problem of learning but may also affect more vital aspects and even lead to the notion of meditation, of philosophical reflections concerning the "beeing" as it is, of an idea of eternal "beeing" and of an eternal circular course, as e.g. the biblical Kohelet expresses (Ecclesiastes or the Preacher): "A generation goes, and a
generation come... be subject and the un贯en down, and hastens to the place where it rises... round round under the wind, and on its circuits the wind returns... its reflections influence the realization of the reproduction of musical drama.

The depth of our researches concerning this theme will show the pedagogical way and some results.)